



UNIVERSITÉ DE TECHNOLOGIE DE BELFORT-MONTBÉLIARD

# Exploration

RO51 - Introduction to Mobile Robotics

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<https://yzrobot.github.io/>

[www.utbm.fr](http://www.utbm.fr)

# What?

- Robotic exploration refers to the exploration of a completely or partially unknown space.
- Objectives of exploration: basic such as mapping ([video](#)), complex such as search and rescue (e.g. finding survivors) and interstellar migration.
- In contrast to SLAM, there is more emphasis on the (full or partial) autonomy of the robot, i.e. answering the question of where should I go.
- Also a fundamental problem in mobile robotics, closer to the public's imagination of robots than the SLAM problem.



# Why?

- There are places where the greatest possible amount of information about the environment should be obtained in advance to ensure human safety, such as caves and mines.
- There are places humans should never go, such as disaster sites (nuclear accidents, fires, etc.)
- Curiosity about the universe.
- And many more.

# How?

- Related to application scenarios and exploration goals.
- Since the problem contains unknowns and a certain degree of requirements for robot autonomy, it can be seen as SLAM plus decision-making from the operational level.
- In addition, the representation of the map (such as occupancy grid map) is a key, as it is an important basis for robot decision-making.

## A brief chronicle before the formal discussion

- 1985: Paper “High Resolution Maps from Wide Angle Sonar” presented by H. Moravec and A. Elfes @ ICRA. => **occupancy grid map**
- 1997: Paper “A Frontier-based Approach for Autonomous Exploration” presented B. Yamauchi @ CIRA. => **frontier-based exploration**
- 2000: Paper “Collaborative multi-robot Exploration” presented W. Burgard *et al.* @ ICRA. => **pioneer work on multi-robot exploration**
- 2002: Paper “Multi-robot Exploration Controlled by a Market Economy” presented R. Zlot *et al.* @ ICRA. => **method developed for MER-A and MER-B**
- 2010: “Sampling-based Multi-robot Exploration” my first scientific paper addresses the problem of exploration waypoint generation for multiple robots.

# Occupancy grid map

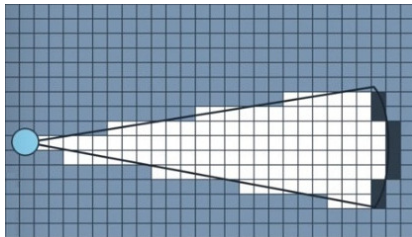
What does it look like?



# Occupancy grid map

What does it look like?

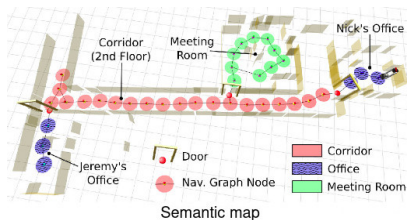
- Use (evenly spaced) grids to represent maps (like some traditional wargames).
- Each grid can have three different states: occupied (obstacle), not occupied (free space), not measured (unknown space).
- The grid state estimate is based on the [posterior probability](#).
- It is a type of [metric map](#) (other metric maps including feature map, point cloud map, etc.).



# Occupancy grid map

## Different maps in mobile robotics

- **Metric map:** Has true physical dimensions, commonly used for SLAM, mapping, localization, and small-scale path planning.
- **Topological map:** Does not have the real physical size, but only represents the connectivity and distance of different locations (e.g subway network), often used for large-scale robot path planning.
- **Semantic map:** Can be seen as a labeled metric map.





# Occupancy grid map

## Why

- **Occupancy:** A cliché: Sensors are not always accurate.
- **Grid:** Modelling continuous spaces is computationally complex and intensive. => discretize the space

# Occupancy grid map

## How

- Commonly used for ranging sensors (e.g. sonar, radar, lidar, etc.).
- Let's look at the algorithm first (a top-down way of thinking):

```

1:   Algorithm occupancy_grid_mapping( $\{l_{t-1,i}\}, x_t, z_t$ ):
2:     for all cells  $m_i$  do
3:       if  $m_i$  in perceptual field of  $z_t$  then
4:          $l_{t,i} = l_{t-1,i} + \text{inverse\_sensor\_model}(m_i, x_t, z_t) - l_0$ 
5:       else
6:          $l_{t,i} = l_{t-1,i}$ 
7:       endif
8:     endfor
9:     return  $\{l_{t,i}\}$ 

```

Courtesy: Probabilistic robotics

# Occupancy grid map

## How

- The goal of an occupancy mapping algorithm is to estimate the **posterior probability** over maps given the data:

$$p(m \mid z_{1:t}, x_{1:t})$$

where  $m$  is the map,  $z_{1:t}$  is the set of measurements from time 1 to  $t$ , and  $x_{1:t}$  is the set of robot poses from time 1 to  $t$ .

- The posterior of a map is approximated by factoring it into:

$$p(m \mid z_{1:t}, x_{1:t}) = \prod_i p(m_i \mid z_{1:t}, x_{1:t})$$

where  $m_i$  denote the grid cell with index  $i$ .

# Occupancy grid map

## How

- $l_{t,j} = \log \frac{p(m_j | z_{1:t}, x_{1:t})}{1 - p(m_j | z_{1:t}, x_{1:t})}$  (a log-odds representation, derivation will be covered in TD)
- **inverse\_sensor\_model**( $\cdot$ ): the inversion of the posterior probability of the state through the result, i.e.

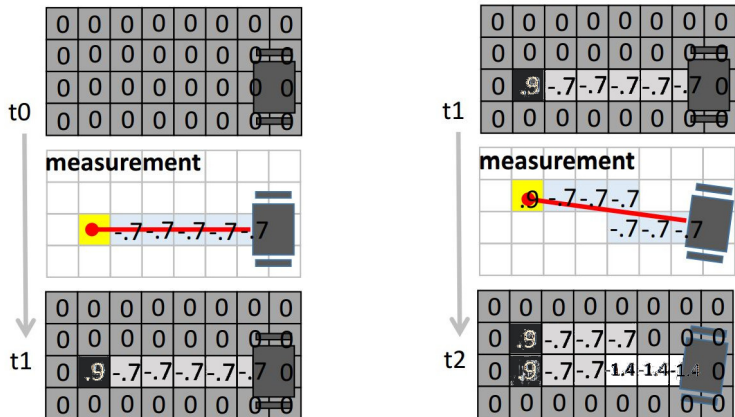
$$\text{inverse\_sensor\_model}(m_i, x_t, z_t) = p(m_i | z_t, x_t)$$

*In human language, the robot has obtained the position of the grid (through measurements), then infers the probability of that grid being occupied.*

- $l_0 = \log \frac{p(m_i=1)}{p(m_i=0)} = \log \frac{p(m_i)}{1-p(m_i)} = \log \frac{0.5}{1-0.5} = 0$  (the constant  $l_0$  is the prior of occupancy represented as a log-odds ratio)

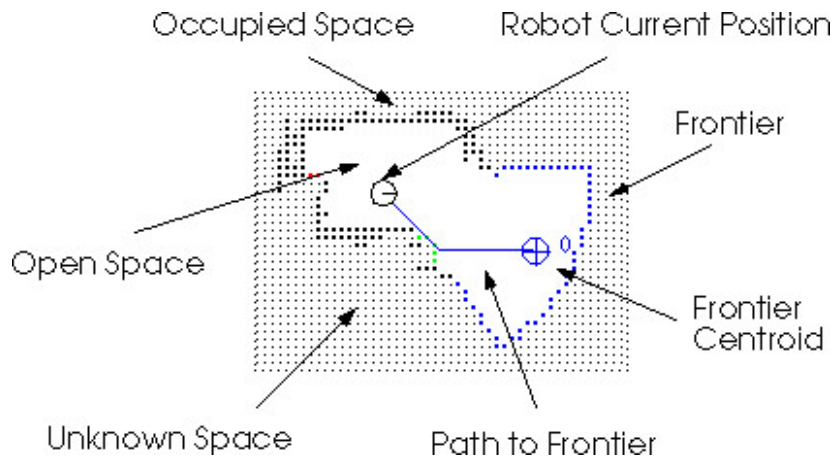
## Occupancy grid map

How

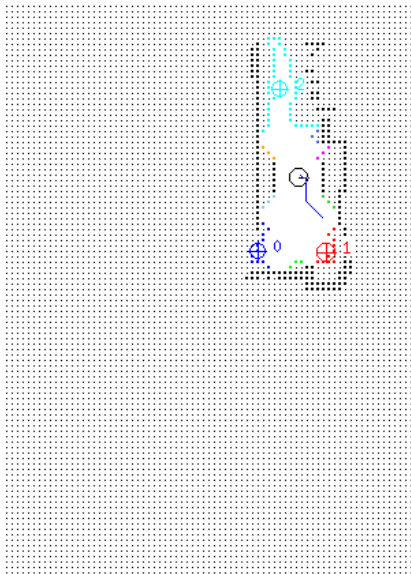


- Just an example:  $l_{free} = -0.7$ ,  $l_{occ} = 0.9$

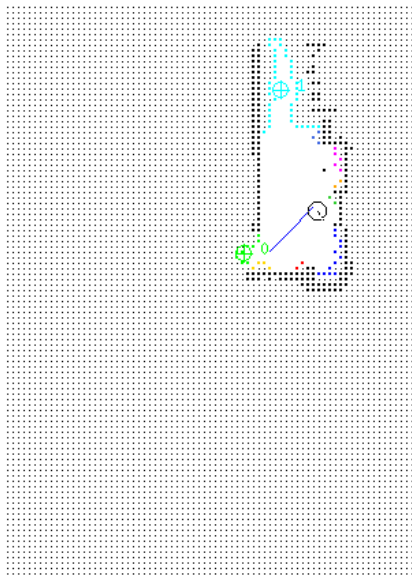
## Frontier-based exploration



## Frontier-based exploration

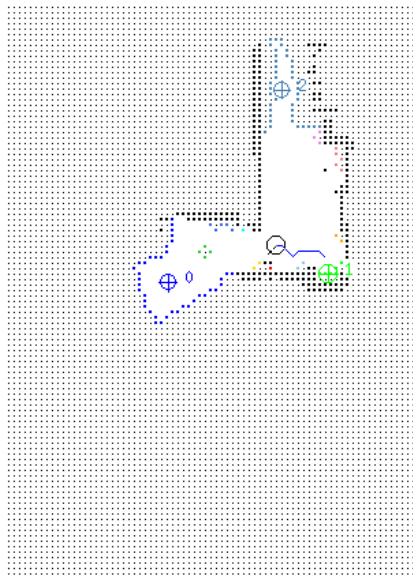


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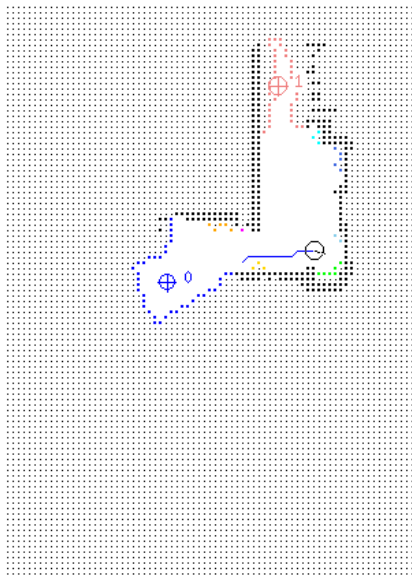




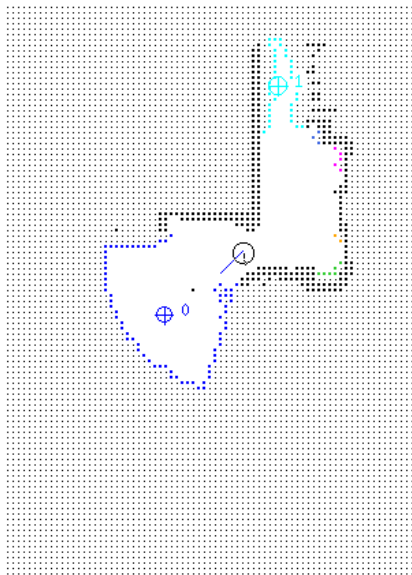
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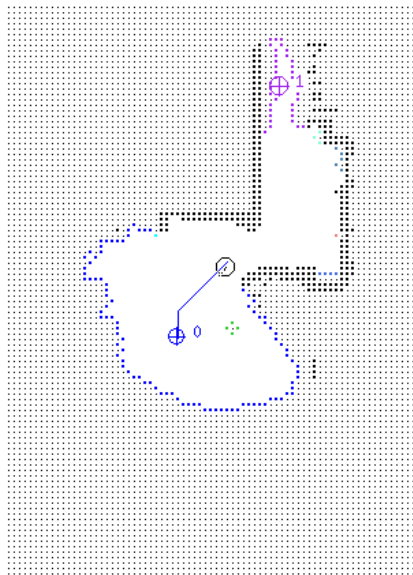
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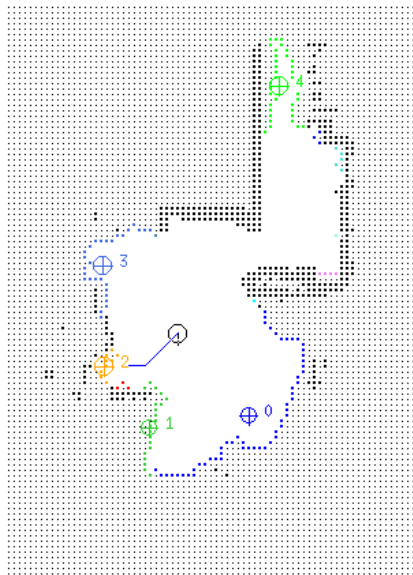
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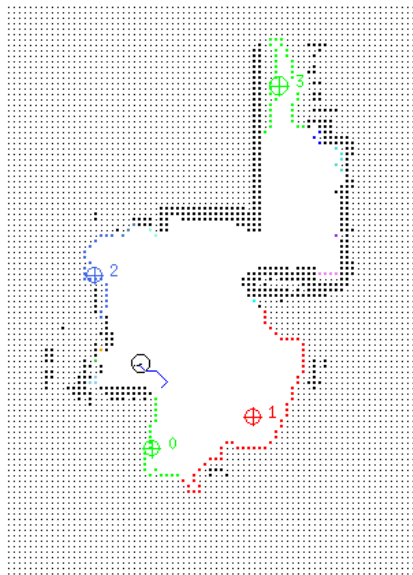
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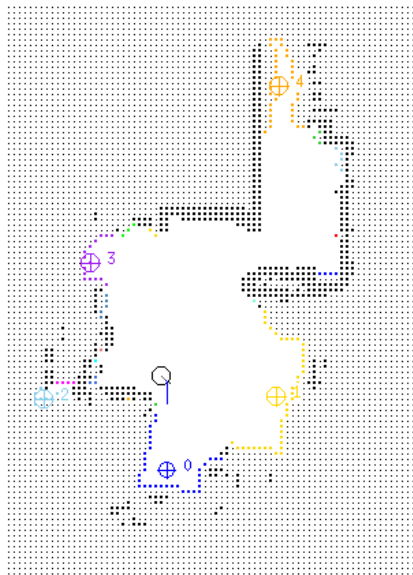
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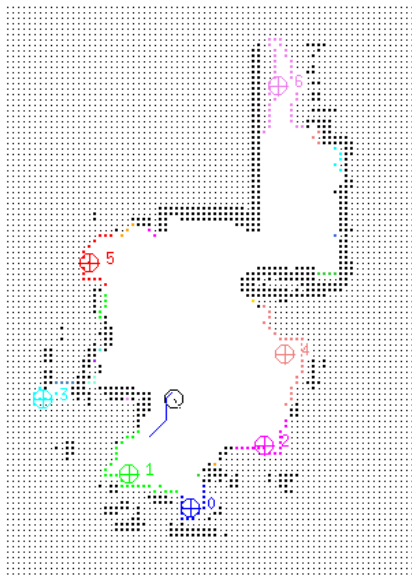
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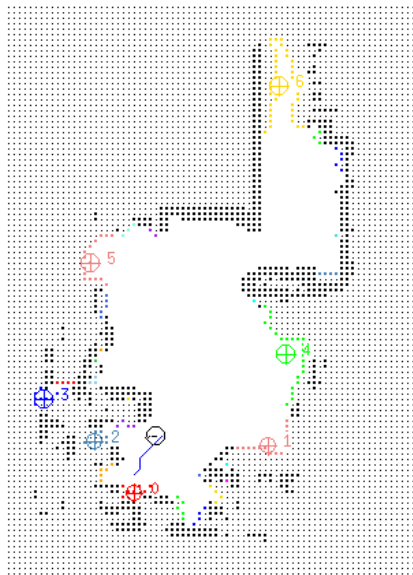


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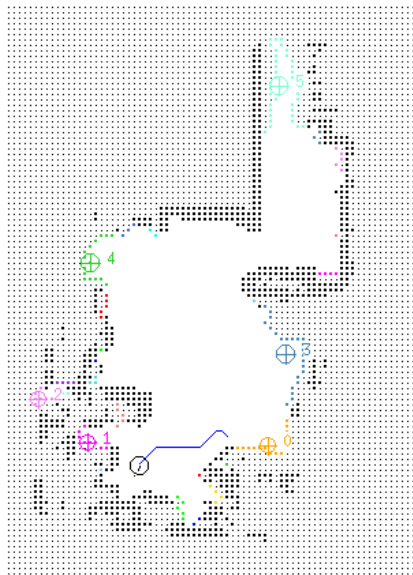




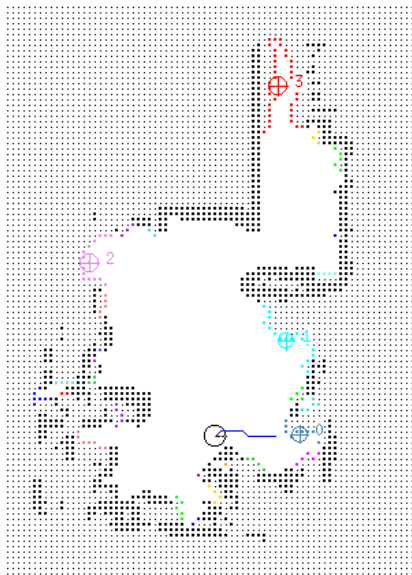
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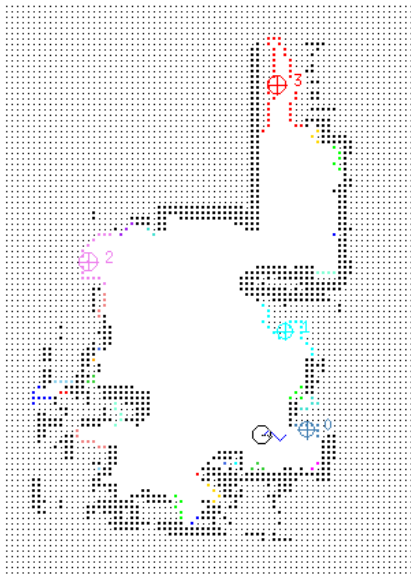
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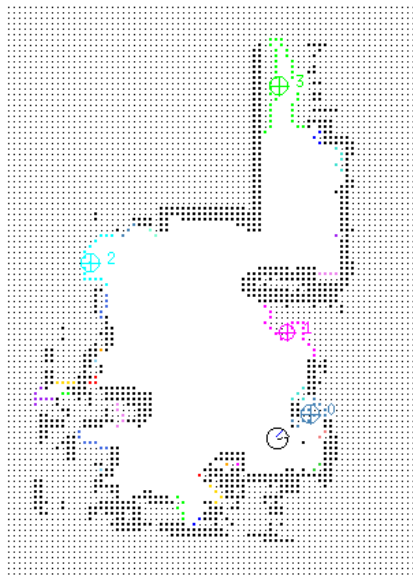
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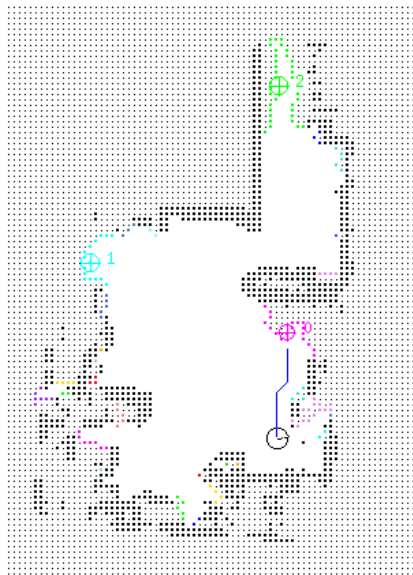
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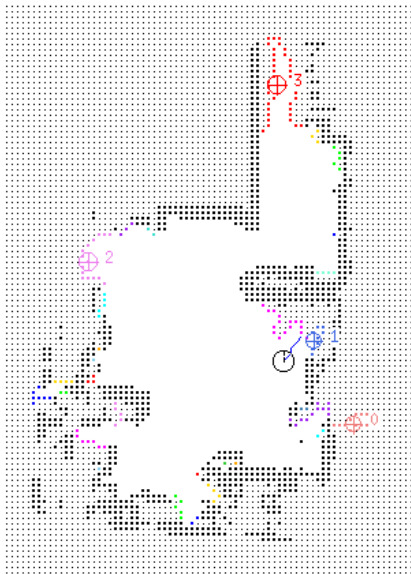
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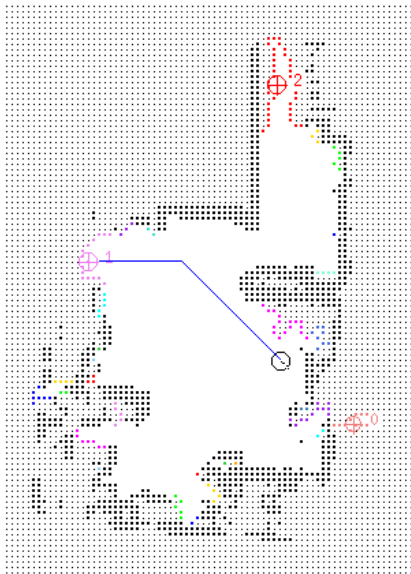
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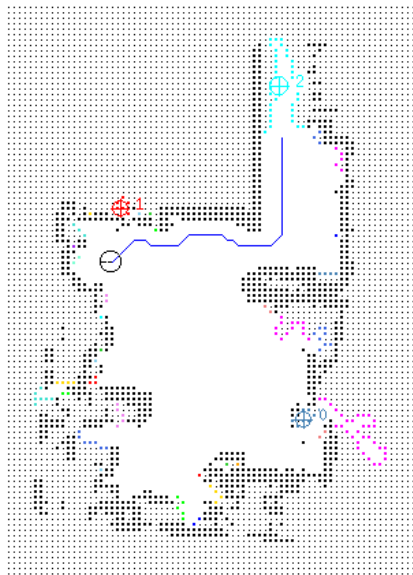


## Frontier-based exploration





## Frontier-based exploration



## Frontier-based exploration

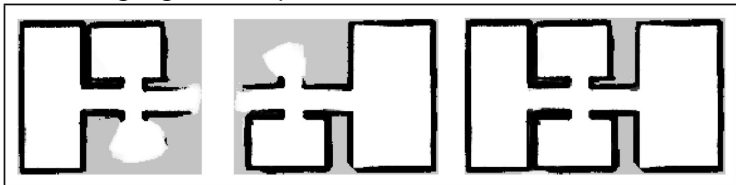
- Judge the method without the background of the times => **non-objective**
- Definition of the frontier: regions on the boundary between open space and unexplored space.
- Method for extracting frontier: similar to edge detection in computer vision.
- A robot does not choose frontiers that cannot be traversed (e.g. based on its physical size).
- If there are multiple frontiers, the robot chooses the closest and unvisited one.
- The robot ends exploration when all frontiers have been visited.

# Multi-robot exploration

- Exploration usually has requirements on time efficiency and energy consumption, because:
  - time is money, time is life,
  - the power of the battery is limited,
- Modern exploration also requires completeness, richness and redundancy (variety) of environmental information.
- Deploying **multi-robot systems** (c.f. Lecture 9) for exploration:
  - Robot team composition (homogeneous or heterogeneous) according to mission needs
  - Cooperative strategy when performing tasks
  - Merging of maps (including communication issues between robots)
  - etc.

# Multi-robot exploration

- Integration of two individual maps (from two mobile robots) into a single global map:



- Suppose there are  $N$  robots which all have an individual map  $m_i$ , and let  $P(occ_{x,y}^i)$  denote the probability that the location  $\langle x, y \rangle$  in the global coordinate frame is occupied in the map of robot  $i$ , then

$$P(occ_{x,y}) = \frac{odds_{x,y}}{1 + odds_{x,y}}$$

where  $odds_{x,y} = \prod_{i=1}^N odds_{x,y}^i$  and  $odds_{x,y}^i = \frac{P(occ_{x,y}^i)}{1 - P(occ_{x,y}^i)}$

## Multi-robot exploration

- Probabilistic fusion of multiple maps: why **odds**, but not addition or multiplication (c.f. Lecture 5)?
  - Addition: different possible outcomes of the same event (e.g. there are multiple methods to complete a task and each method can complete this task independently).
  - Multiplication: different steps of the same event (e.g. it takes  $n$  steps to complete a task).
  - Odds: provides a measure of the likelihood of a particular outcome and takes into account multi-sensor interactions (for the derivation process, see Moravec's classic paper published in 1988: *Sensor Fusion in Certainty Grids for Mobile Robots*).

# Multi-robot exploration

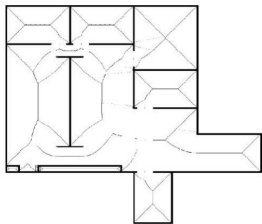
Task allocation: **Contract Net Protocol (CNP)**, a task-sharing protocol introduced in 1980 by Reid G. Smith:

- ① The protocol is initialized by a task manager, who sends a call-for-proposals to the contractors.
- ② The contractors can send either a proposal if they are interested or a reject if they are not.
- ③ The manager chooses among the proposals the one that suits it best, and sends to the corresponding contractor an accept.
- ④ Once the contract has been accomplished, the contractor informs the manager using an inform message.

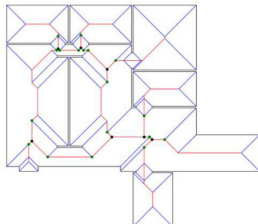
	Market-based approach	Auction-based approach	Trade-based approach
<b>Negotiation (communication) model</b>	publish / subscribe	publish / subscribe	apply / allocate
<b>Task allocation algorithm</b>	greedy algorithm (first-price auction)	greedy algorithm (first-price auction)	greedy algorithm (first-price auction)
<b>Task allocation ability per iteration (trading round)</b>	single task	single task	multiple tasks
<b>Role determination of the robots</b>	voluntary	voluntary	negotiation
<b>Utility consideration</b>	cost and benefit	cost	cost
<b>Task reassignment</b>	allowed	not allowed	allowed
<b>Communication complexity</b>	$O(1)$ / bidder, $O(n)$ / auctioneer	$O(1)$ / bidder, $O(n)$ / auctioneer	$O(1)$ / buyer, $O(n)$ / seller
<b>Computation complexity</b>	$O(n)$	$O(n)$	$O(n)$

# Completely vs. partially unknown spaces

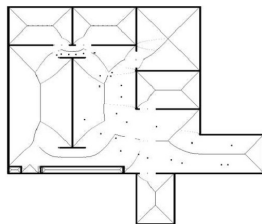
- **Completely unknown space:** the robot (not human) does not have any information (a priori) about the target environment.
- **Partially unknown space:** the robot has partial information about the target environment, such as a floor plan.
  - This is often very useful for search and rescue missions.



Voronoi Diagram



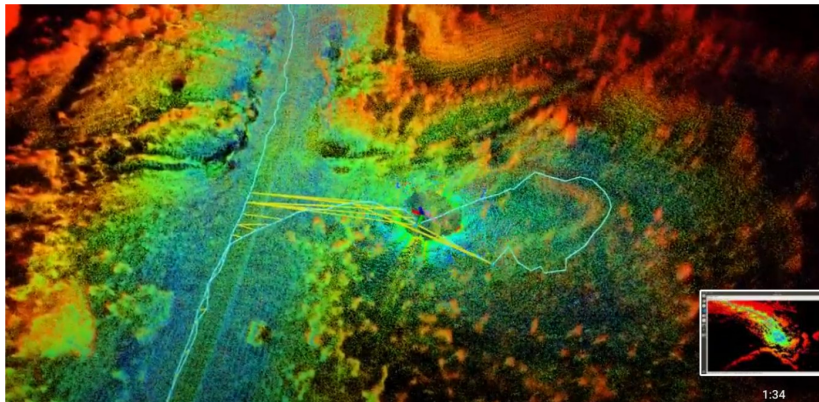
Straight Skeleton



Sampling-Based

# Structured vs. unstructured environments

- **Structured environment:** building interior
- **Unstructured environment:** fields, mines, Mars, etc.



Lidar mapping in field test at Longshaw National Trust



# Rover@UTBM project

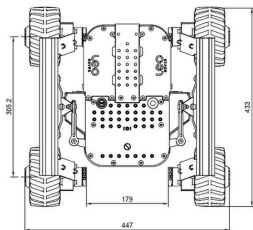
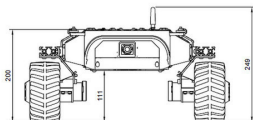
In a Mars-like environment:

- The road situation is very complex. => **challenging the stability of the robot locomotion** (c.f. Lecture 2)
- It is difficult to rely solely on ranging sensors (e.g. lidar, radar, sonar) to explore. => **lack of landmarks and sensor readings**



## Rover@UTBM project

## Size and performance

**Size**

Weight: 6,5 kg  
 Dimensions: 447x433x249 mm  
 Payload capacity: ca. 5 kg

**Upper platform mounting dimensions**

Dimensions: 299 x 183 mm  
 Hole grid: 18 x 15 mm  
 Holes: 40 x  $\Phi$  7mm + 22 x  $\Phi$  5,5mm

**Performance**

Estimated maximum obstacle size: 70 mm  
 Protection rating: complies with IP66 (not certified)

Run time: Estimated 4 hrs of nominal driving

Connection range: Up to 100m (with live video stream)

**Camera**

Camera resolution: 5 MPx  
 Lens: Fisheye with 170 deg field of view (IR non-filtered; night-vision allowed)

**Network**

WiFi 2.4 GHz access point with external antenna  
 WiFi 2.4 GHz + 5 GHz on internal RPi antennas for connectivity

**Wheels**

Motors: 4 x in-hub DC motor with 73.21 planetary gearbox and 12 CPR encoder  
 Wheel diameter: 130 mm  
 Tire material: rubber with foam insert (non-pneumatic)

**Battery**

Voltage: 11.1 V DC  
 Capacity: 5000 mAh  
 Type: Li-Ion with internal PCM  
 Short-circuit, overcurrent and overdrain safety features  
 Max. current: 8A (total for the whole Rover)

**Speed**

Max. linear speed: ca. 0.4 m/s  
 Max. angular speed: ca. 60 deg/s

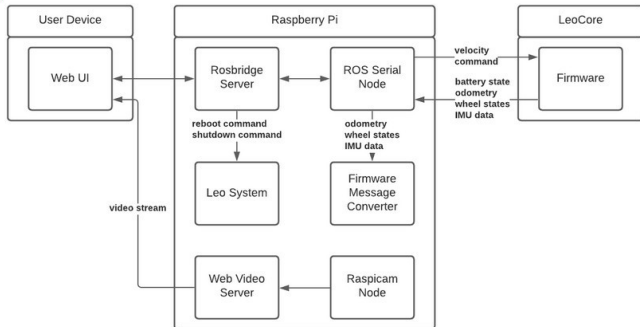
## Rover@UTBM project

## Software

Operating system: Ubuntu 20.04 + Robot Operating System

Ready-to-go UI located under '10.0.0.1' when using standard Leo Software Image.

Open source firmware



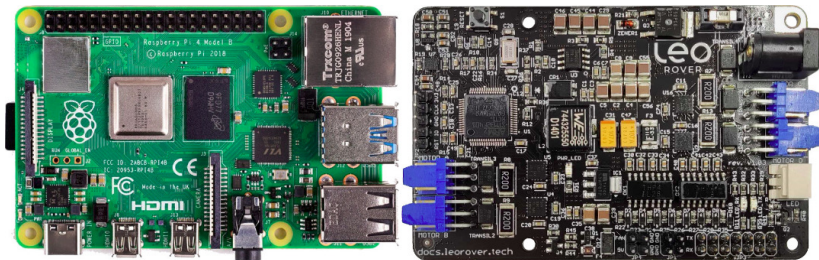
## Electronics

RaspberryPi 4B 2GB (or higher) as the main computer

LeoCore as real-time microcontroller: STM32F4 (@84MHz, 64KB RAM, 256KB Flash)

# Rover@UTBM project

- Higher level control (like cerebrum): Raspberry Pi, running Linux and ROS.
- Lower level control (like cerebellum): LeoCore board, running firmware (C/C++), providing:
  - differential drive controller (*cmd\_vel* interface)
  - wheel states monitoring (*joint\_states* interface)
  - battery voltage monitoring
  - wheel odometry calculation
  - IMU support



## Rover@UTBM project

- The outer diameter of the tires affects the rover's speed and force (slope/climbing ability).
  - higher outer diameter = higher speed & lower force
  - lower outer diameter = lower speed & higher force
- The stiffness of the tires affects the rover's turning resistance and ability to climb obstacles.



$$\text{Rover Speed [m/s]} = \frac{\text{wheel diameter [m]} \times \pi \times \text{motor speed [rpm]}}{60}$$

$$\text{Rover Force [N]} = \frac{4 \times \text{motor torque [Nm]}}{\text{wheel diameter [m]}}$$

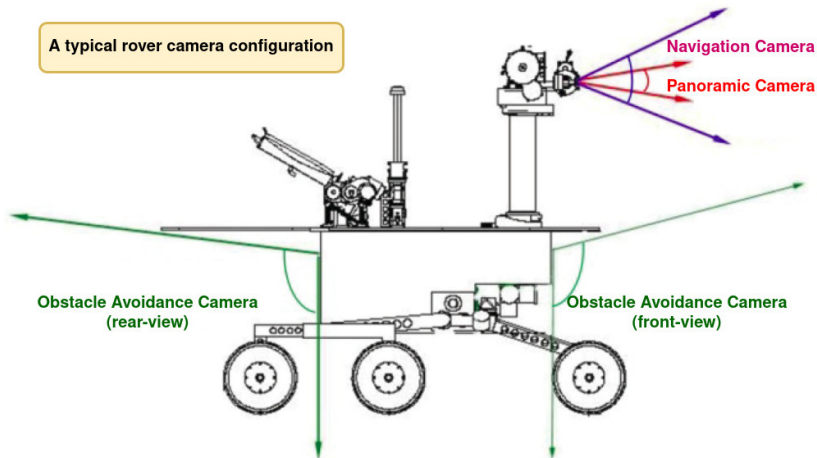
# Mars rover

## Landed rover

Landing date	Rover name	Active duration	Main sensor
1997-7-4	Sojourner (USA)	85 days	2x gray & 1x color cameras 5x laser stripe projectors
2004-1-4	Spirit / MER-A (USA)	2249 days	4x different cameras 1x thermal spectrometer
2004-1-25	Opportunity / MER-B (USA)	5250 days	4x different cameras 1x thermal spectrometer
2012-8-6	Curiosity (USA)	still operational	17x different cameras
2021-2-18	Perseverance (USA)	still operational	19x different cameras 2x microphones
2021-5-15	Zhurong (China)	still operational	4x different cameras 1x ground-penetrating radar

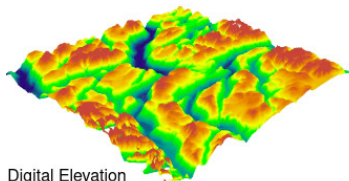
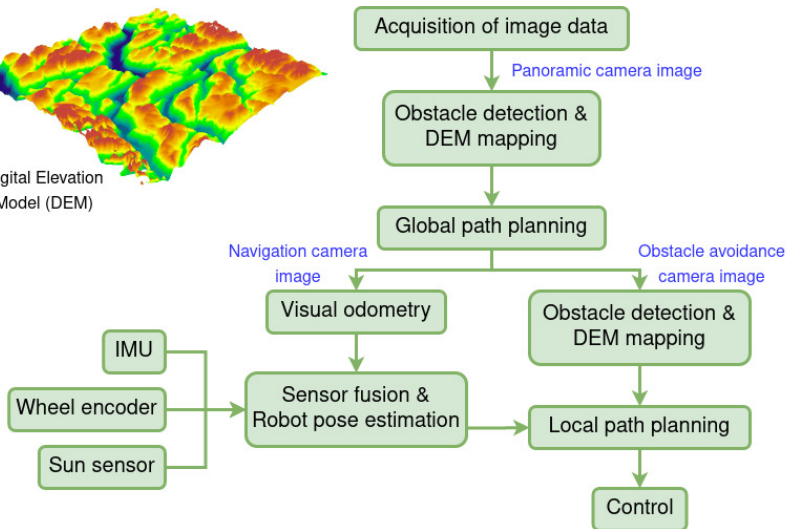
# Mars rover

Cameras rule, lidar step aside



## Mars rover

## Basic flowchart of the exploration system

Digital Elevation  
Model (DEM)



# Summary

- Exploration: what, why and how.
- Occupancy grid map, frontier-based exploration, multi-robot exploration.
- Rover@UTBM project.
- The practice of exploration will be covered in TD and TP.
- This lecture pays more attention to cultivating students' interest in mobile robotics, especially its application in space exploration.
- Let's wrap up today's lecture with a [video](#).

# The end

Thank you for your attention!

Any questions?